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## Crystal Structure

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## $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$, a lyonsite molybdate

## Daniel E. Bugaris and Hans-Conrad zur Loye*

Department of Chemistry and Biochemistry, University of South Carolina, 631
Sumter Street, Columbia, SC 29208, USA
Correspondence e-mail: zurloye@mailbox.sc.edu

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Trilithium aluminium trimolybdate $(\mathrm{VI}), \mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$, has been grown as single crystals from $\alpha-\mathrm{Al}_{2} \mathrm{O}_{3}$ and $\mathrm{MoO}_{3}$ in an $\mathrm{Li}_{2} \mathrm{MoO}_{4}$ flux at 998 K . This compound is an example of the well known lyonsite structure type, the general formula of which can be written as $A_{16} B_{12} \mathrm{O}_{48}$. Because this structure can accomodate cationic mixing as well as cationic vacancies, a wide range of chemical compositions can adopt this structure type. This has led to instances in the literature where membership in the lyonsite family has been overlooked when assigning the structure type to novel compounds. In the title compound, there are two octahedral sites with substitutional disorder between $\mathrm{Li}^{+}$and $\mathrm{Al}^{3+}$, as well as a trigonal prismatic site fully occupied by $\mathrm{Li}^{+}$. The $(\mathrm{Li}, \mathrm{Al}) \mathrm{O}_{6}$ octahedra and $\mathrm{LiO}_{6}$ trigonal prisms are linked to form hexagonal tunnels along the [100] axis. These polyhedra are connected by isolated $\mathrm{MoO}_{4}$ tetrahedra. Infinite chains of face-sharing $(\mathrm{Li}, \mathrm{Al}) \mathrm{O}_{6}$ octahedra extend through the centers of the tunnels. A mixed $\mathrm{Li} / \mathrm{Al}$ site, an Li , an Mo , and two O atoms are located on mirror planes.

## Comment

Although its namesake mineral, $\alpha-\mathrm{Cu}_{3} \mathrm{Fe}_{4}\left(\mathrm{VO}_{4}\right)_{6}$, was not structurally characterized until much later (Hughes et al., 1987), the lyonsite crystal structure was first observed in 1964 in $\mathrm{NaCo}_{2.31}\left(\mathrm{MoO}_{4}\right)_{3}$ (Ibers \& Smith, 1964). An excellent review of this structure type was published recently (Smit et al., 2006). The general formula for the lyonsite family of compounds can be written as $A_{16} B_{12} \mathrm{O}_{48}$ [or $A_{16}\left(B \mathrm{O}_{4}\right)_{12}$ or $A_{4}\left(B \mathrm{O}_{4}\right)_{3}$ ]. The $A$ cations, with octahedral and trigonal prismatic coordination environments, most commonly have formal oxidation states of $1+, 2+$, or $3+$, though some examples have been found with cations in higher oxidation states, such as $\mathrm{Ti}^{4+}$ (Smit et al., 2008) and $\mathrm{Nb}^{5+}$ (Smit et al., 2006). The tetrahedral $B$ cations in lyonsite consist exclusively of $\mathrm{V}^{5+}$, $\mathrm{Mo}^{6+}$ and $\mathrm{W}^{6+}$. Typically, there is a mixture of two cations on the $A$ site, or sometimes cationic vacancies, in order to preserve overall electroneutrality.

The lyonsite crystal structure (Fig. 1) features isolated $\mathrm{BO}_{4}$ tetrahedra which are interconnected by $A \mathrm{O}_{6}$ octahedra and


Figure 1
Polyhedral representation of the lyonsite crystal structure type. (In the electronic version of the paper, edge-sharing $A \mathrm{O}_{6}$ octahedra are shown in blue, face-sharing $A \mathrm{O}_{6}$ octahedra in brown, $A \mathrm{O}_{6}$ trigonal prisms in green and $\mathrm{BO}_{4}$ tetrahedra in gray.)
trigonal prisms. The octahedra and trigonal prisms form hexagonal tunnels in the [100] direction. The $\mathrm{BO}_{4}$ tetrahedra line the interior of these tunnels, and infinite chains of facesharing $A \mathrm{O}_{6}$ octahedra extend through the centers of the tunnels. The $A O_{6}$ octahedra in the hexagonal tunnels share edges to form columns, while the $A \mathrm{O}_{6}$ trigonal prisms share edges to form zigzag sheets. When there are multiple $A$ cations, the larger ones tend to be localized on the more geometrically accommodating trigonal prismatic site. Because the face-sharing octahedra in the infinite chains possess the shortest $A \cdots A$ interatomic distances, cationic vacancies, when present, are concentrated on this site to reduce coulombic repulsions.

The title compound crystallizes in the space group Pnma of the orthorhombic system with the lyonsite structure type. Previously, only the unit-cell parameters of $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$ had been reported on the basis of indexing of powder X-ray diffraction data (Klevtsov, 1970). Here, we report the first high-quality single-crystal X-ray diffraction structure determination. The crystals were prepared by a high-temperature solution reaction where $\mathrm{Li}_{2} \mathrm{MoO}_{4}$ served as the flux. Alkali molybdates are commonly used as flux for the growth of single crystals of complex molybdenum-containing oxides (Bugaris \& zur Loye, 2012).

In $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$ (Fig. 2), the $B$ sites are occupied by $\mathrm{Mo}^{6+}$ cations tetrahedrally coordinated by oxide anions. The $\mathrm{Mo}-\mathrm{O}$ bond lengths in the title compound are in the range 1.7244 (17)-1.7937 (16) $\AA$ [average 1.766 (5) Å]. These interatomic distances are consistent with those for the isostructural compound $\mathrm{Li}_{3} \mathrm{Ga}\left(\mathrm{MoO}_{4}\right)_{3}$ (van der Lee et al., 2008), which are in the range $1.734(2)-1.795(2) \AA$. The $\mathrm{O}-\mathrm{Mo}-\mathrm{O}$ angles of 104.01 (12)-116.13 (12) ${ }^{\circ}$ correspond to a nearly regular $\mathrm{MoO}_{4}$ tetrahedron.


Figure 2
Ball-and-stick representation of the crystal structure of $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$, as viewed down [100]. \{In the electronic version of the paper, the blue spheres are $\mathrm{Li}^{+}$and $\mathrm{Al}^{3+}$ cations [mixed sites with 72.1 (2):27.9 (2)\% occupancy, respectively], the brown spheres are $\mathrm{Li}^{+}$and $\mathrm{Al}^{3+}$ cations [mixed sites with 55.8 (5):44.2 (4)\% occupancy, respectively], the green spheres are $\mathrm{Li}^{+}$cations, the gray spheres are $\mathrm{Mo}^{6+}$ cations and the red spheres are $\mathrm{O}^{2-}$ anions.\}

The $A$ cationic sites in the title compound are occupied by a mixture of $\mathrm{Li}^{+}$and $\mathrm{Al}^{3+}$ cations in the $3: 1$ ratio necessary to preserve charge electroneutrality. The trigonal prismatic sites are occupied completely by $\mathrm{Li}^{+}$cations, while the octahedral sites are occupied by a mixture of $\mathrm{Li}^{+}$and $\mathrm{Al}^{3+}$ cations. The edge-sharing ${A \mathrm{O}_{6} \text { octahedra in the hexagonal tunnels contain }}^{2}$ $72.1(2) \% \mathrm{Li}^{+}$, while the face-sharing $A \mathrm{O}_{6}$ octahedra in the infinite chains contain 55.8 (5) $\% \mathrm{Li}^{+}$. As the ionic radius of sixcoordinate $\mathrm{Al}^{3+}$ is significantly smaller than that of six-coordinate $\mathrm{Li}^{+}(0.535 \AA$ versus $0.76 \AA$; Shannon, 1976), it is to be expected that a higher percentage of $\mathrm{Al}^{3+}$ is found on the facesharing octahedral site in order to alleviate Coulombic repulsions. No $\mathrm{Al}^{3+}$ is found on the trigonal prismatic site, consistent with the fact that this site is more accomodating towards a larger cation, in this case $\mathrm{Li}^{+}$. A similar separation of large and small cations into trigonal prismatic and octahedral sites is observed in the 2 H -perovskite-related oxide structure type (zur Loye et al., 2012).

Other compounds belonging to the $\mathrm{Li}_{3} M^{3+}\left(\mathrm{MoO}_{4}\right)_{3}$ family of compounds with the lyonsite structure type exhibit disorder of the $\mathrm{Li}^{+}$and $M^{3+}$ cations on the $A$ sites. The edge-sharing $A \mathrm{O}_{6}$ octahedral sites contain 70 (1), 69.2 (1), 66.67, 71.91 (17) and $75 \%$ of $\mathrm{Li}^{+}$, while the face-sharing $A \mathrm{O}_{6}$ octahedral sites contain 56 (1), 61.7 (1), 66.67, 57.9 (3) and $58 \%$ of $\mathrm{Li}^{+}$, for $M=$ $\mathrm{V}^{3+}$ (Mikhailova et al., 2010), $\mathrm{Cr}^{3+}$ (Sarapulova et al., 2009), $\mathrm{Fe}^{3+}$ (Klevtsova \& Magarill, 1970), $\mathrm{Ga}^{3+}$ (van der Lee et al.,
2008) and $\mathrm{Sc}^{3+}$ (Kolitsch \& Tillmanns, 2003), respectively. With regard to the examples containing $\mathrm{V}^{3+}, \mathrm{Cr}^{3+}, \mathrm{Fe}^{3+}$ and $\mathrm{Ga}^{3+}$, the trigonal prismatic site is occupied entirely by $\mathrm{Li}^{+}$. For $\mathrm{Li}_{3} \mathrm{Sc}\left(\mathrm{MoO}_{4}\right)_{3}$, the trigonal prismatic site contains $92 \% \mathrm{Li}^{+}$ and $8 \% \mathrm{Sc}^{3+}$. The appearance of $\mathrm{Sc}^{3+}$ on the trigonal prismatic site can be attributed to the larger ionic radius of six-coordinate $\mathrm{Sc}^{3+}(0.745 \AA)$, which is approaching the size of sixcoordinate $\mathrm{Li}^{+}$. The ionic radii of six-coordinate $\mathrm{Cr}^{3+}$ $(0.615 \AA), \mathrm{Ga}^{3+}(0.62 \AA), \mathrm{V}^{3+}(0.64 \AA)$ and $\mathrm{Fe}^{3+}(0.645 \AA)$ are significantly smaller than that of $\mathrm{Li}^{+}$, so as in the title compound, none of these cations is found on the trigonal prismatic site.

In $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$, the $\mathrm{Li} / \mathrm{Al}-\mathrm{O}$ bond lengths in the edgesharing octahedra are in the range 2.003 (2) -2.143 (3) $\AA$. For the face-sharing octahedra, the $\mathrm{Li} / \mathrm{Al}-\mathrm{O}$ interatomic distances are in the range 1.957 (2)-2.023 (3) $\AA$. The bond lengths are shorter for the face-sharing octahedra because a higher concentration of the smaller $\mathrm{Al}^{3+}$ cation is found on those sites. Finally, the $\mathrm{Li}-\mathrm{O}$ interatomic distances in the trigonal prisms are in the range 2.103 (5)-2.222 (6) Å.

The Li-ion conductivity of various Li-containing lyonsite materials has been investigated for their potential application as electrolyte materials in Li-ion batteries (Sebastian et al., 2003). It was determined that, although the lyonsite crystal structure is a three-dimensional framework, the conduction pathway of the $\mathrm{Li}^{+}$ions is limited to the zigzag sheets of edgesharing trigonal prisms. Therefore, it is to be expected that compounds with a greater concentration of $\mathrm{Li}^{+}$on the trigonal prismatic sites would exhibit higher ionic conductivities. For example, the ionic conductivities measured for $\mathrm{Li}_{3} \mathrm{Cr}\left(\mathrm{MoO}_{4}\right)_{3}$ and $\mathrm{Li}_{3} \mathrm{Fe}\left(\mathrm{MoO}_{4}\right)_{3}$ were higher than those of the $\mathrm{Li}_{2-2 x} \mathrm{Mg}_{2+x}\left(\mathrm{MoO}_{4}\right)_{3}$ series of compounds. In the $\mathrm{Cr}-$ and Fe-containing materials, the trigonal prismatic sites are fully occupied by $\mathrm{Li}^{+}$, whereas in the Mg -containing materials the trigonal prismatic sites are occupied by a mixture of $\mathrm{Li}^{+}$and $\mathrm{Mg}^{2+}$. It would be interesting to measure the ionic conductivity of the title compound, $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$, which contains only $\mathrm{Li}^{+}$ on the trigonal prismatic sites, in order to ascertain whether the ionic conductivity is comparable with or higher than the $\mathrm{Cr}-\mathrm{and} \mathrm{Fe}$-containing materials.

## Experimental

Colorless prismatic crystals of $\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$ were grown from a mixture of $\mathrm{Li}_{2} \mathrm{MoO}_{4}$ (Alfa Aesar, $99+\%$ ), $\alpha-\mathrm{Al}_{2} \mathrm{O}_{3}$ (Alfa Aesar, $99.9 \%$ ) and $\mathrm{MoO}_{3}$ (Alfa Aesar, $99.95 \%$ ). The $\mathrm{Li}_{2} \mathrm{MoO}_{4}$ was dried overnight at 423 K to remove any adsorbed water. The starting reagents $\alpha-\mathrm{Al}_{2} \mathrm{O}_{3}(0.10196 \mathrm{~g}, 1 \mathrm{mmol})$, and $\mathrm{MoO}_{3}(0.14394 \mathrm{~g}$, $1 \mathrm{mmol})$, with $\mathrm{Li}_{2} \mathrm{MoO}_{4}(0.43455 \mathrm{~g}, 2.5 \mathrm{mmol})$ acting as both a source of Li and a flux, were ground together thoroughly using a mortar and pestle. The mixture was transferred to an alumina crucible, covered loosely and placed in a furnace. The mixture was heated at a rate of $200 \mathrm{~K} \mathrm{~h}^{-1}$ to 998 K , where it was held for 12 h , before being cooled at a rate of $2 \mathrm{~K} \mathrm{~h}^{-1}$ to 773 K , at which point it was allowed to cool rapidly to room temperature. The excess lithium molybdate flux was removed by washing with hot water, aided by sonication, and colorless prismatic crystals of the title compound were isolated by vacuum filtration.

Table 1
Selected bond lengths (Å).

| Li1-O5 | 2.003 (2) | Li3- $\mathrm{O6}^{\text {v }}$ | 2.103 (5) |
| :---: | :---: | :---: | :---: |
| Li1-O5 ${ }^{\text {i }}$ | 2.025 (2) | $\mathrm{Li} 3-\mathrm{O} 7^{\text {vi }}$ | 2.168 (5) |
| Li1-O6 | 2.029 (2) | $\mathrm{Li} 3-\mathrm{O}^{\text {i }}$ | 2.168 (5) |
| $\mathrm{Li} 1-\mathrm{O} 2^{\text {ii }}$ | 2.061 (2) | $\mathrm{Li} 3-\mathrm{O} 7{ }^{\text {vii }}$ | 2.222 (6) |
| Li1-O3 | 2.093 (2) | $\mathrm{Li} 3-\mathrm{O} 7{ }^{\text {viii }}$ | 2.222 (6) |
| $\mathrm{Li} 1-\mathrm{O} 2{ }^{\text {i }}$ | 2.143 (3) | $\mathrm{Mo} 1-\mathrm{O} 2$ | 1.7550 (17) |
| $\mathrm{Li} 2-\mathrm{O} 4^{\text {iii }}$ | 1.957 (2) | $\mathrm{Mo} 1-\mathrm{O} 2^{\text {v }}$ | 1.7550 (17) |
| $\mathrm{Li} 2-\mathrm{O} 4^{\text {iv }}$ | 1.957 (2) | Mo1-O3 | 1.781 (3) |
| $\mathrm{Li} 2-\mathrm{O}^{\text {v }}$ | 1.965 (2) | Mo1-O1 | 1.781 (2) |
| Li2-O4 | 1.965 (2) | Mo2-O7 | 1.7244 (17) |
| $\mathrm{Li} 2-\mathrm{O} 1^{\text {iv }}$ | 2.018 (3) | Mo2-O6 ${ }^{\text {ix }}$ | 1.7595 (17) |
| Li2-O1 | 2.023 (3) | Mo2-O5 | 1.7770 (17) |
| Li3-O6 | 2.103 (5) | $\mathrm{Mo} 2-\mathrm{O} 4^{\mathrm{x}}$ | 1.7937 (16) |

Symmetry codes: (i) $-x,-y,-z+1$; (ii) $x-1, y, z$; (iii) $x+\frac{1}{2},-y+\frac{1}{2},-z+\frac{1}{2}$; (iv) $x+\frac{1}{2}, y,-z+\frac{1}{2}$; (v) $x,-y+\frac{1}{2}, z$; (vi) $-x, y+\frac{1}{2},-z+1$; (vii) $-x-\frac{1}{2}, y+\frac{1}{2}, z+\frac{1}{2}$; (viii) $-x-\frac{1}{2},-y, z+\frac{1}{2}$; (ix) $-x-1,-y,-z+1 ;$ (x) $x-\frac{1}{2}, y,-z+\frac{1}{2}$.

## Crystal data

$\mathrm{Li}_{3} \mathrm{Al}\left(\mathrm{MoO}_{4}\right)_{3}$
$M_{r}=527.62$
Orthorhombic, Pnma
$a=5.0372(10) \AA$
$b=10.320(2) \AA$
$c=17.272(4) \AA$

$$
\begin{aligned}
& V=897.8(3) \AA^{3} \\
& Z=4 \\
& \text { Mo } K \alpha \text { radiation } \\
& \mu=4.29 \mathrm{~mm}^{-1} \\
& T=298 \mathrm{~K} \\
& 0.07 \times 0.07 \times 0.05 \mathrm{~mm}
\end{aligned}
$$

## Data collection

## Bruker SMART APEX CCD areadetector diffractometer

Absorption correction: numerical (SADABS; Sheldrick, 2008) $T_{\text {min }}=0.661, T_{\text {max }}=0.746$

## Refinement

| $R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.021$ | 99 parameters |
| :--- | :--- |
| $w R\left(F^{2}\right)=0.048$ | 4 restraints |
| $S=1.12$ | $\Delta \rho_{\max }=0.80 \mathrm{e} \AA^{-3}$ |
| 1606 reflections | $\Delta \rho_{\min }=-0.76 \mathrm{e}^{-3}$ |

A model with substitutional disorder between Li and Al was proposed for this compound. Similar disorder was observed in the isostructural compounds $\mathrm{Li}_{3} M^{3+}\left(\mathrm{MoO}_{4}\right)_{3}(M=\mathrm{V}, \mathrm{Cr}, \mathrm{Fe}, \mathrm{Ga}, \mathrm{Sc})$. The occupancies of the Li1/Al1 and Li2/Al2 crystallographic sites were constrained to 1.00 , whereas restraints with an s.u. value of 0.001 were used for keeping the total number of Li atoms in the structural formula at 3.0 and the total number of Al atoms in the structural formula at 1.0 , i.e. occupancy $(\operatorname{Li} 1)+0.5 \times \operatorname{occupancy}(\mathrm{Li} 2)=1.0$, and occupancy $(\mathrm{Al} 1)+0.5 \times \operatorname{occupancy}(\mathrm{Al} 2)=0.5$. There is no evidence
in the refinement for the presence of Al on the trigonal prismatic site ( $100 \% \mathrm{Li}$ ).

The largest positive and negative residual electron densities of 0.804 and -0.763 e $\AA^{-3}$ are located 0.76 and $0.58 \AA$, respectively, from atom Mo1.

Data collection: SMART (Bruker, 2001); cell refinement: SMART; data reduction: SAINT-Plus (Bruker, 2001); program(s) used to solve structure: SHELXS97 (Sheldrick, 2008); program(s) used to refine structure: SHELXL97 (Sheldrick, 2008); molecular graphics: CrystalMaker (Palmer, 2012); software used to prepare material for publication: SHELXTL97 (Sheldrick, 2008).

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Supplementary data for this paper are available from the IUCr electronic archives (Reference: KU3069). Services for accessing these data are described at the back of the journal.

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